

Recursion

Recursion is when a function can call itself; either directly or indirectly.

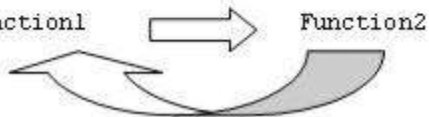
- Direct recursion is when a function calls itself

Function1



- Indirect recursion is when a function calls another function; and the process can later call one of the prior functions; function1 calls function2 which then calls function1.

Function1



Recursion must have

- A terminating point and
- The algorithm of the recursion must move to that point.

The following is an example of a factorial function.

5! is $5 \times 4 \times 3 \times 2 \times 1$

5! can also be thought of as $5 \times 4!$

4! can be thought of as $4 \times 3!$ And so forth

```
using namespace std;
#include <iostream>
```

```
int factorial(int n);
```

```
int main ()
```

```
{ int n =5;
  cout << factorial(5);           // Initial value of 5!
  return 0;
}
```

```
//-----
```

```
int factorial(int n)
{ if (n==1)                // The bottom or terminating point
  return (1);
  else return(factorial(n-1)*n);  //Recursion occurs here !! The function calls itself

                                //The algorithm now multiplies n*(n-1)!
}
```

The next section shows how the stack works for a factorial call for 3!.

Memory location	Value	identifier
4		
3		
2	3	n
1	Unknown so far but will be $3 * 2!$	factorial

Pushes onto stack like a cafeteria stack of trays
Current Activation (call #1)

n	Location 2	Value is 3
---	------------	------------

factorial	Location 1	Unknown so far but will be $3 * 2!$
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Memory location	Value	identifier
4	2	n
3	Unknown so far but will be $2 * 1!$	factorial
2	3	n
1	Unknown so far but will be $3 * 2!$	factorial

Pushes onto stack like a cafeteria stack of trays
Current Activation (call #2)

n	Location 4	Value is 2
---	------------	------------

factorial	Location 3	Unknown so far but will be $2 * 1!$
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Memory location	Value	identifier
6	1	n
5	Returns a value of 1	factorial
4	2	n
3	Unknown so far but will be $2 * 1!$	factorial
2	3	n
1	Unknown so far but will be $3 * 2!$	factorial

Pushes onto stack like a cafeteria stack of trays
Current Activation (call #3)

n	Location 6	Value is 1
---	------------	------------

factorial	Location 5	Returns a value of 1
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Memory location	Value	identifier
6	1	n
5	Returns a value of 1	factorial
4	2	n
3	Returns a value of 2	factorial
2	3	n
1	Unknown so far but will be $3 * 2!$	factorial

Memory location	Value	identifier
6	1	n
5	Returns a value of 1	factorial
4	2	n
3	Returns a value of 2	factorial
2	3	n
1	Returns a value of $6 (3 * 2!)$	factorial

Pops off the stack like a cafeteria stack of trays
Returns to Prior Activation (call #2)

n	Location 4	Value is 2
factorial	Location 3	Returns a value of $1 * 2!$

Notice that values on the stack are not deleted; this fact is a major reason that you must initialize variables!!!

Pops off the stack like a cafeteria stack of trays
Returns to Prior Activation (call #1)

n	Location 2	Value is 3
factorial	Location 1	Returns a value of $3 * 2!$